

Elementary Number Theory Continuation And Polynom Academic PDF

Elementary number theory continuation and polynom form an intriguing intersection in the realm of mathematics, offering insights into the properties of integers and the behaviors of polynomial functions over various domains. This exploration deepens our understanding of divisibility, modular arithmetic, and polynomial functions, providing foundational tools for advanced mathematical concepts and applications in cryptography, coding theory, and algebraic structures.

Introduction to Elementary Number Theory and Polynomials

Elementary number theory is a branch of pure mathematics dealing with the properties and relationships of integers. It encompasses concepts such as divisibility, prime numbers, greatest common divisors, and modular arithmetic. Polynomials, on the other hand, are algebraic expressions involving variables and coefficients, fundamental to algebra and calculus.

Understanding how polynomial functions behave over integers and modular systems is essential for various applications. The continuation of elementary number theory into the study of polynomials helps in solving congruences, understanding polynomial roots in modular arithmetic, and analyzing polynomial factorization over different fields.

Fundamental Concepts in Elementary Number Theory

Divisibility and Prime Numbers

Divisibility is a core concept, where an integer a divides another integer b if there exists an integer k such that $b = ak$. Prime numbers are those greater than 1 that have no divisors other than 1 and themselves.

Greatest Common Divisor (GCD) and Least Common Multiple (LCM)

The GCD of two integers is the largest integer dividing both, while the LCM is the smallest number divisible by both. These concepts are vital in simplifying fractions and solving Diophantine equations.

Modular Arithmetic

This system considers integers with respect to a modulus n , where two numbers are equivalent if their difference is divisible by n . Modular arithmetic is foundational in cryptography and computer

science.

Polynomial Functions in Number Theory

Definition and Basic Properties

A polynomial function involves variables raised to non-negative integer powers with coefficients in a given field, typically the integers or rationals. For example:

$$P(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$

where (a_i) are coefficients.

Polynomials over Integers and Modular Systems

Studying polynomials over $(\mathbb{Z})$ (the integers) and $(\mathbb{Z}/n\mathbb{Z})$ (integers modulo (n)) reveals rich structures:

- Roots of polynomials modulo (n)
- Polynomial factorization in modular systems
- Solutions to polynomial congruences

Elementary Number Theory and Polynomial Congruences

Polynomial Congruences

A polynomial congruence is an expression like:

$$P(x) \equiv 0 \pmod{n}$$

which seeks integers (x) satisfying the congruence. Solving such congruences is fundamental in number theory and has applications in cryptography and coding theory.

Methods of Solving Polynomial Congruences

To solve polynomial congruences, mathematicians use various techniques:

- **Factoring Polynomials:** Break down polynomials into products of lower-degree polynomials to find roots.
- **Hensel's Lemma:** Lift solutions modulo (p) to solutions modulo (p^k) , where (p) is prime.
- **Chinese Remainder Theorem:** Combine solutions modulo coprime factors of (n) to find solutions modulo (n) .

Polynomial Factorization in Number Theory

Irreducible Polynomials

A polynomial over a field is irreducible if it cannot be factored into polynomials of lower degree with coefficients in that field. Identifying irreducible polynomials is crucial for understanding polynomial extensions and roots.

Factorization over Finite Fields

Finite fields, such as $(\mathbb{F}_p)$, the field with (p) elements, enable the factorization of polynomials in a finite setting. This is essential for constructing error-correcting codes and cryptographic algorithms.

Applications of Elementary Number Theory and Polynomials

Cryptography

Number theory underpins many cryptographic protocols:

- RSA encryption relies on properties of prime numbers and modular exponentiation.
- Elliptic curve cryptography uses polynomial equations over finite fields.

Coding Theory

Error-correcting codes, such as Reed-Solomon codes, are based on polynomial evaluations over finite fields, ensuring data integrity in communication systems.

Algebraic Number Theory and Galois Theory

Polynomials and their roots over various fields lead to the development of Galois theory, which studies symmetries of roots and solvability of polynomial equations.

Advanced Topics in Number Theory and Polynomials

Diophantine Equations

These are polynomial equations seeking integer solutions, such as Fermat's Last Theorem:

$\mathbb{Z}$

$$x^n + y^n = z^n$$

$\mathbb{Z}$

which has no solutions for $(n > 2)$.

Number Fields and Polynomial Extensions

Studying roots of polynomials in algebraic extensions of $(\mathbb{Q})$ (the rationals) leads to the concept of algebraic number fields, crucial in modern number theory.

Analytic Number Theory and L-Functions

Connections between prime distributions and zeros of polynomial-related functions, such as Dirichlet L-functions, reveal deep properties of numbers.

Conclusion

The continuation of elementary number theory into the study of polynomials unlocks a broad spectrum of mathematical insights. From solving polynomial congruences to factorization over finite fields, these concepts form the backbone of numerous theoretical and practical advancements. Understanding the interplay between integers and polynomial functions enriches our grasp of algebra, number theory, and their applications, paving the way for innovations in cryptography, coding theory, and beyond.

By exploring these topics, mathematicians develop tools to approach complex problems involving divisibility, primality, and polynomial equations, demonstrating the timeless relevance and depth of elementary number theory and polynomials in modern mathematics.

Elementary Number Theory Continuation and Polynomials

Elementary number theory forms the foundation of many advanced mathematical concepts and applications, from cryptography to algebraic geometry. When we talk about the continuation of elementary number theory and its interplay with polynomials, we delve into a realm that combines the simplicity of basic divisibility and prime concepts with the richness of polynomial algebra. This synthesis not only deepens our understanding of number theoretic structures but also opens pathways to more sophisticated areas such as algebraic number theory, Diophantine equations, and modular forms. In this article, we explore the core ideas, recent developments, and practical implications of continuing elementary number theory with polynomial techniques, providing a comprehensive overview for both students and seasoned mathematicians.

Understanding Elementary Number Theory and Its Continuation

Elementary number theory primarily deals with the properties and relationships of integers, focusing on concepts such as divisibility, prime numbers, greatest common divisors, and modular arithmetic. Its simplicity makes it accessible, yet its depth offers endless avenues for exploration. When we consider the continuation of elementary number theory, we are looking at how these fundamental ideas extend into more complex structures and how polynomial methods can enhance our understanding.

The Core Concepts of Elementary Number Theory

Before discussing continuation, it's crucial to revisit the core concepts:

- Divisibility and primes: Understanding how numbers divide each other and the role of prime numbers.
- Greatest common divisor (GCD) and least common multiple (LCM): Essential for understanding divisibility relationships.
- Modular arithmetic: Working with integers modulo a number, crucial for cryptography.
- Fundamental Theorem of Arithmetic: Every integer greater than 1 can be uniquely factored into primes.
- Diophantine equations: Polynomial equations seeking integer solutions.

Why Continue Elementary Number Theory?

The motivation for continuing elementary number theory lies in its limitations when faced with more complex problems. While it provides a solid base, many problems require tools beyond basic divisibility?enter polynomials. The transition to polynomial methods allows us to:

- Factorize more complex structures.

- Solve higher-degree equations.
- Understand algebraic structures that underpin number theory.

Polynomials in Number Theory

Polynomials serve as powerful tools in number theory, providing a bridge between algebraic concepts and arithmetic properties. By studying polynomials over various domains—integers, rational numbers, finite fields—we unlock new insights into divisibility, factorization, and the distribution of primes.

Polynomial Concepts Relevant to Number Theory

- Polynomial rings: Sets of polynomials with coefficients in a given domain, such as $\mathbb{Z}[x]$ or $\mathbb{F}_p[x]$.
- Irreducible polynomials: Analogous to prime numbers in integers; key in factorization.
- Roots and factorization: Understanding roots over different fields sheds light on polynomial divisibility.
- Polynomial congruences: Equations like $f(x) \equiv 0 \pmod{n}$ relate directly to modular arithmetic.
- Eisenstein's Criterion: A test for irreducibility of polynomials, useful for constructing irreducible polynomials.

The Significance of Polynomial Techniques

In number theory, polynomials enable us to:

- Construct number fields and study their properties.
- Analyze the distribution of prime ideals via polynomial factorizations.
- Formulate and solve Diophantine equations.
- Investigate the structure of finite fields, which are fundamental in coding theory and cryptography.

Key Topics in the Continuation of Elementary Number Theory with Polynomials

- Polynomial Factorization and Primes

Understanding how polynomials factor over various fields is crucial. For example, irreducible

polynomials over finite fields correspond to minimal polynomials of algebraic elements, and their factorization patterns influence the structure of field extensions.

Features & Applications:

- Construction of finite fields: $\mathbb{F}_{p^n}$ via irreducible polynomials over $\mathbb{F}_p$.
- Cryptographic algorithms: Use of irreducible polynomials to generate pseudorandom sequences.
- Coding theory: Polynomial factorization helps in designing error-correcting codes.
- Polynomial Congruences and Roots

Solving polynomial congruences like $f(x) \equiv 0 \pmod{n}$ is a natural extension of modular arithmetic. The solutions to such equations are closely related to the structure of the underlying rings and fields.

Features & Applications:

- Use in RSA: Polynomial equations mod n relate to factorization.
- Cryptography: Polynomial root-finding over finite fields underpins many encryption schemes.
- Number-theoretic functions: Example?using polynomials to generate multiplicative characters.
- Cyclotomic Polynomials and Roots of Unity

Cyclotomic polynomials $\Phi_n(x)$ encapsulate the primitive n -th roots of unity. Their properties link to prime distributions and Galois theory.

Features & Applications:

- Connection to prime numbers: Irreducibility over $\mathbb{Q}$ and prime factorization.
- Galois groups: Symmetries of roots relate to field automorphisms.
- Cryptography: Cyclotomic fields used in lattice-based cryptography.
- Diophantine Equations and Polynomial Methods

Many classical problems in number theory involve solving polynomial equations in integers. Polynomial techniques, including factorization, reduction, and the application of algebraic number theory, are vital.

Features & Applications:

- Fermat's Last Theorem: Proven using algebraic number theory and elliptic curves.
- Pell's Equation: Connection to quadratic polynomials and units in quadratic fields.
- Modern algorithms: Use of polynomial factorization algorithms in computational number theory.

Recent Developments and Advanced Topics

While the core ideas are classical, recent research continues to expand how polynomials are used in number theory:

- Polynomial method in additive combinatorics: Techniques like the polynomial method have solved longstanding problems in combinatorics and number theory.
- Use in cryptography: Advances in polynomial-based cryptosystems such as lattice cryptography.
- Algorithmic developments: Improved algorithms for polynomial factorization over finite fields and integers, impacting computational number theory.

Pros and Cons of Using Polynomial Methods in Number Theory

Pros:

- Versatility: Applicable across various branches of algebra, geometry, combinatorics.
- Structural insights: Polynomials reveal deep structural properties of number fields and rings.
- Algorithmic efficiency: Polynomial factorizations are computationally feasible with modern algorithms.
- Connections to other fields: Bridging number theory with algebraic geometry, coding theory, and cryptography.

Cons:

- Complexity: Polynomial problems can become computationally intensive, especially over large fields.

- Field dependence: Results often depend heavily on the underlying field or ring; generalizations can be non-trivial.
- Abstractness: Advanced polynomial techniques may be inaccessible to beginners without substantial background.

Conclusion

The continuation of elementary number theory through polynomial methods enriches both the theoretical landscape and practical applications. From fundamental concepts like irreducibility and factorization to sophisticated tools used in cryptography and algebraic geometry, polynomials serve as a unifying language that extends the reach of classical number theory. As computational techniques improve and theoretical insights deepen, the interplay between elementary concepts and polynomial algebra promises to remain at the forefront of mathematical innovation. Whether you're exploring prime distributions, solving Diophantine equations, or designing secure cryptosystems, understanding how polynomials augment number theory is invaluable. This ongoing synthesis not only preserves the elegance of elementary ideas but also pushes the boundaries of what we can achieve in modern mathematics.

Question What is the significance of polynomial factorization in elementary number theory? Polynomial factorization helps in understanding the divisibility properties of polynomials over integers and finite fields, which can be used to solve Diophantine equations and analyze prime distributions within polynomial values. How does the concept of polynomial roots relate to elementary number theory? Polynomial roots, especially over integers or finite fields, are crucial in number theory for identifying solutions to polynomial equations, understanding irreducibility, and exploring properties like quadratic residues and primitive roots. What is the role of Eisenstein's criterion in polynomial irreducibility within number theory? Eisenstein's criterion provides a sufficient condition for a polynomial to be irreducible over the integers, which is essential for studying prime polynomials and their factorization properties in algebraic number theory. How can polynomial congruences be used to solve number theoretic problems? Polynomial congruences help in solving equations modulo primes or composite numbers, enabling the analysis of quadratic residues, primitive roots, and the distribution of solutions, which are key topics in elementary number theory. What is the application of continuation methods in polynomial approximation within number theory? Continuation methods, such as homotopy continuation, are used to approximate roots of polynomials, especially in complex cases, aiding in computational number theory tasks like finding integer solutions or analyzing polynomial behavior. In what way do polynomials relate to the distribution of prime numbers in elementary number theory? Polynomials like Euler's polynomial or the polynomial generating primes in certain sequences are studied to understand prime distribution, and their properties can provide insights or conjectures related to prime density and patterns. What are some common techniques for continuing solutions of polynomial equations in number theory? Techniques include Hensel lifting for p-adic solutions, Newton-Raphson iterations for numerical approximations, and algebraic continuation methods, all used to extend solutions from known points

to broader contexts in number theory.

Related keywords: elementary number theory, polynomials, divisibility, modular arithmetic, prime numbers, polynomial functions, integer solutions, congruences, algebraic structures, polynomial roots

AN INTRODUCTION TO ERGODIC THEORY GRADUATE TEXTS I

An introduction to ergodic theory graduate texts i serves as a foundational guide for graduate students venturing into this fascinating branch of mathematics. Ergodic theory, at its core, explores the long-term average behavior of dynamical systems and their statistical properties. It has profound applications across mathematics, physics, and even in fields like economics and computer science. For students beginning their journey, selecting the right graduate texts is crucial for building a solid understanding, developing intuition, and engaging with current research directions. This article aims to provide a comprehensive overview of essential ergodic theory texts, their key features, and how they can serve as effective learning tools.

Understanding the Foundations of Ergodic Theory

Before diving into specific texts, it's important to understand what ergodic theory encompasses and why it's a vital area of study. This section offers a brief overview of the fundamental concepts and the scope of graduate-level texts.

What is Ergodic Theory?

Ergodic theory studies the behavior of measure-preserving transformations on probability spaces. Essentially, it addresses questions like: How do points in a dynamical system distribute over time? Do the time averages of functions along trajectories converge to space averages? These questions are rooted in the ergodic hypothesis, which originated from statistical mechanics.

Key concepts include:

- Measure-preserving transformations
- Ergodicity and mixing
- Invariant measures
- Birkhoff's Ergodic Theorem
- Unique ergodicity

Understanding these ideas lays the groundwork for exploring more advanced topics covered in graduate texts.

Essential Graduate Texts in Ergodic Theory

Choosing the right textbooks is essential for mastering ergodic theory. The following sections highlight some of the most influential and widely recommended graduate-level texts, discussing their strengths and targeted audiences.

1. "An Introduction to Ergodic Theory" by Peter Walters

Walters' book is often considered a classic starting point for graduate students.

Key features:

- Clear and rigorous presentation
- Focuses on measure-theoretic foundations
- Covers fundamental theorems such as Birkhoff's and von Neumann's
- Includes numerous exercises for practice

This text is ideal for students new to the field, providing a solid theoretical foundation before moving to more specialized topics.

2. "Ergodic Theory" by Karl Petersen

Petersen's work is comprehensive and slightly more advanced.

Key features:

- Emphasizes both measure-theoretic and topological dynamics
- Discusses entropy, mixing, and applications
- Contains detailed proofs and examples
- Suitable for students with some background in measure theory and topology

This book bridges foundational concepts with more recent developments, making it a good next step after Walters.

3. "Introduction to Ergodic Theory" by Ya. G. Sinai

Sinai's text offers a blend of intuition and formalism.

Key features:

- Focuses on the intuition behind the theorems
- Connects ergodic theory with statistical mechanics
- Includes historical notes and motivations
- Suitable for students who prefer a conceptual approach

Additional Resources and Advanced Texts

Graduate students aiming to deepen their understanding should explore more specialized and advanced texts. Here are some noteworthy options:

1. "Ergodic Theory and Differentiable Dynamics" by Anatole Katok and Boris Hasselblatt

This comprehensive volume covers a broad spectrum of topics.

Highlights:

- Smooth ergodic theory
- Hyperbolic systems and Anosov diffeomorphisms
- Structural stability
- It is suitable for students interested in the interface between ergodic theory and differential dynamics.

2. "Measure Theory and Probability" by Malcolm Adams and Victor Guillemin

While broader in scope, this book provides valuable measure-theoretic background essential for advanced ergodic theory.

Strategies for Studying Ergodic Theory Graduate Texts

Mastering ergodic theory requires more than just reading; active engagement is key. Here are some tips for making the most of these texts:

- **Start with the basics:** Ensure a solid understanding of measure theory, topology, and

functional analysis.

- **Work through exercises:** Practice problems reinforce concepts and develop problem-solving skills.
- **Supplement with lectures and seminars:** Engage with online courses or university seminars for different perspectives.
- **Form study groups:** Discussing complex topics with peers enhances understanding.
- **Connect theory to applications:** Explore how ergodic theory applies to physics, information theory, and other fields.

Conclusion

An introduction to ergodic theory graduate texts provides a roadmap for students embarking on this mathematical journey. Starting with foundational books like Walters' "An Introduction to Ergodic Theory" offers an accessible entry point, while advanced texts like Katok and Hasselblatt's work open doors to current research areas. By selecting appropriate resources, actively engaging with the material, and connecting theory with applications, students can develop a deep and lasting understanding of ergodic theory. Whether your interest lies in pure mathematics, statistical mechanics, or dynamical systems, the right graduate texts are invaluable tools for your academic and research pursuits in ergodic theory.

An Introduction to Ergodic Theory Graduate Texts: A Comprehensive Guide for Students and Enthusiasts

Embarking on the study of ergodic theory graduate texts opens a gateway to a rich and profound branch of mathematics that intersects dynamical systems, measure theory, probability, and statistical mechanics. For graduate students venturing into this field, selecting the right textbooks can significantly influence their understanding and appreciation of the subject. This guide aims to shed light on the foundational texts, their structure, strengths, and how they serve as stepping stones into the depths of ergodic theory.

Understanding the Foundations of Ergodic Theory

Before diving into specific texts, it's crucial to grasp what ergodic theory entails. At its core, ergodic theory studies the long-term average behavior of dynamical systems with an invariant measure. Its applications range from statistical physics and information theory to number theory and chaos theory.

Key concepts include:

- Measure-preserving transformations

- Invariant measures
- Ergodicity and mixing
- Birkhoff's Ergodic Theorem
- Ornstein's theory of Bernoulli flows

Graduate texts in ergodic theory typically assume familiarity with measure theory, topology, and basic dynamical systems, making it a challenging yet rewarding subject for advanced students.

The Landscape of Graduate Texts in Ergodic Theory

Choosing a graduate-level textbook involves understanding its approach, prerequisites, and depth. The major texts in the field can generally be categorized based on their focus: foundational theory, applications, or a blend of both.

Classic and Seminal Texts

- "Ergodic Theory" by Peter Walters

- Overview: Widely regarded as a definitive introductory textbook, Walters' "Ergodic Theory" is praised for clarity, rigorous proofs, and comprehensive coverage.
- Scope: It covers measure-preserving transformations, ergodic decomposition, mixing properties, and entropy.
- Strengths:
 - Well-structured for graduate courses
 - Emphasizes the connection between measure theory and dynamics
 - Includes numerous examples and exercises
- Prerequisites: Measure theory, basic topology, and some familiarity with dynamical systems.

- "An Introduction to Ergodic Theory" by Peter Walters

- Often considered the go-to text for graduate students or advanced undergraduates beginning the subject.
- Focuses on core concepts with detailed proofs.
- Suitable as a primary textbook or supplementary resource.

Advanced and Specialized Texts

- "Ergodic Theory via Joinings" by Eli Glasner

- Overview: Focuses on joinings, a sophisticated tool in ergodic theory, providing a modern perspective.
- Audience: More suitable for students who have already mastered the basics and want to explore advanced topics.
- Features: Incorporates recent developments, emphasizing the structural and classification aspects of ergodic systems.

- "Entropy, Large Deviations, and Statistical Mechanics" by David Ruelle

- While broader in scope, this text delves into the thermodynamic formalism, a key area in ergodic theory.
- Ideal for students interested in the applications of ergodic theory in statistical physics.

Textbooks with a Focus on Applications or Interdisciplinary Approaches

- "Ergodic Theory: with a view towards Number Theory" by Manfred Einsiedler and Thomas Ward

- Overview: Connects ergodic theory with number theory, providing applications to problems like equidistribution and primes.
- Features: Combines rigorous theory with motivating applications, making it accessible and engaging.

How to Choose the Right Graduate Text in Ergodic Theory

When selecting a textbook, consider the following factors:

- Prerequisites: Ensure you have a solid background in measure theory and topology.
- Focus Area: Decide whether you want a foundational understanding or a focus on particular applications.
- Depth: Some texts offer a broad overview, while others delve into specialized topics.
- Teaching Style: Supplementary materials, exercises, and clarity of exposition can greatly impact your learning.

Recommended approach:

- Start with Walters' "Ergodic Theory" for a comprehensive foundation.
- Use other texts, like Glasner's "Ergodic Theory via Joinings," for advanced topics.
- Supplement with research papers and lecture notes for recent developments.

Structuring Your Study of Ergodic Theory

To maximize your understanding, consider a structured approach:

- Build a Strong Measure Theory Foundation
 - Review measure spaces, sigma-algebras, and integration.
 - Study probability theory basics, as ergodic theory often involves probabilistic concepts.
- Understand Dynamical Systems
 - Familiarize yourself with topological and measurable dynamics.
 - Explore examples like rotations, shifts, and hyperbolic systems.
- Dive into Core Ergodic Concepts
 - Invariant measures and ergodicity
 - Birkhoff's Ergodic Theorem
 - Mixing properties and their implications
- Explore Advanced Topics
 - Entropy theory
 - Ornstein's isomorphism theorem
 - Joinings and structural classification
 - Connections with number theory and statistical mechanics

Supplementary Resources and Learning Strategies

- Lecture series: Many universities offer free lecture notes; for example, the lecture series by Peter Walters or others available online.
- Problem sets: Practice through exercises in textbooks or problem books.
- Research papers: Engage with current developments by reading papers in journals like Ergodic Theory and Dynamical Systems.
- Discussion groups: Join seminars or study groups focused on ergodic theory.

Conclusion

An introduction to ergodic theory graduate texts is essential for anyone aiming to master the subject at an advanced level. The journey begins with foundational texts like Peter Walters' "Ergodic Theory," which offers clarity and depth, and then progresses into more specialized or application-driven materials. By understanding the structure, prerequisites, and scope of these texts, students can tailor their learning path effectively. With dedication, rigorous study, and engagement with supplementary materials, mastering ergodic theory becomes an achievable and intellectually rewarding pursuit.

Final Tips

- Be patient: The subject is challenging but immensely rewarding.
- Connect theory with examples: Visualize systems like rotations or shifts.
- Engage actively: Solve problems and participate in discussions.
- Keep abreast of current research: This enriches your understanding and opens new avenues.

Embark on this mathematical voyage with confidence?ergodic theory offers profound insights into the behavior of complex systems and the nature of randomness and order in mathematics.

Question What is the primary focus of 'An Introduction to Ergodic Theory' by Peter Walters? The book provides a rigorous introduction to ergodic theory, focusing on measure-preserving transformations, ergodic theorems, and their applications in dynamical systems and statistical mechanics. Which prerequisites are recommended before studying this text? A solid background in measure theory, real analysis, and basic topology is recommended to fully grasp the concepts presented in the book. How does the book approach the topic of ergodic theorems? It systematically introduces the mean and pointwise ergodic theorems, providing proofs and discussing their implications in the context of dynamical systems. Are there applications of ergodic theory discussed in this graduate text? Yes, the book explores applications such as statistical properties of dynamical systems, mixing, and entropy, illustrating how ergodic theory connects to

various fields. Is this book suitable for self-study or primarily for classroom use? While designed as a graduate textbook, it is also suitable for self-study due to its clear explanations, though some background in measure theory is helpful. What makes 'An Introduction to Ergodic Theory' by Walters a trending choice among graduate texts? Its comprehensive coverage, clear exposition, and balance between theory and applications have made it a popular and influential resource in the field of ergodic theory.

Related keywords: ergodic theory, measure theory, dynamical systems, invariant measures, ergodicity, mixing, entropy, Birkhoff's theorem, stationary processes, ergodic decomposition

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